

# Deficits, public debt dynamics, and tax and spending multipliers

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- What are the **effects of fiscal austerity**?
- General point: the effects of any given instrument adjustment are **never unambiguously defined** unless we **define the policy regime** in which the adjustment occurs
- Paper calculates effects of short-run and long-run fiscal adjustments
  - Under various financing assumptions
  - Decomposes direct and indirect effects
- Paper compares how fiscal effects change when interest rates hit their lower bound
  - At zero bound, fiscal adjustments may have powerful effects on output
  - Warning: in severe crisis, cutting public spending or raising taxes **may increase the deficit**

- The standard New Keynesian pieces:
  - IS curve; AS curve
  - (Sticky prices, flexible wages, no physical capital)
- Government budget constraint:
  - Public spending, income taxes, consumption taxes, lump sum taxes
  - Nominal public debt
- Monetary policy:
  - Inflation peg
  - Subject to zero lower bound

- Crisis scenario
  - Shock to discount factor alters natural real interest rate
  - Zero lower bound may bind
- Simplified infinite-horizon timing
  - “Short run”: Persistent preference shock lowers natural interest rate
  - “Short run” ends with probability  $1 - \mu$  per period
  - “Long run”: deterministic
- Study effects of fiscal adjustments
  - Compare adjustments of spending and taxes
  - Compare nonbinding/binding ZLB in short run
  - Distinguish direct short-run effects of fiscal adjustments ...
  - ... from the effects associated with financing those adjustments

First study effects of short-run changes in instruments, without any further distortions.

- **(1). Change one fiscal instrument in the short run**, balance budget by adjusting lump sum taxes
  - Change spending, income taxes, or consumption taxes
  - Calculate short-run effects on output, deficit...
  - ... conditional on nonbinding/binding zero lower bound

# Indirect budgetary effects of policy changes

Next, study policy adjustments required for long-term budget balance.

- **(2A.) Change one fiscal instrument in the long run**, balance budget by adjusting lump sum taxes
  - Calculate long-run effects on output
  - Calculate short-run effects on output and deficit with/without ZLB
- **(2B.) Faster debt growth in the short run**, then bring debt back to steady state in long run by **exponentially declining adjustment of one fiscal instrument**
  - Fix long-run half-life of deviations from steady state
  - Calculate long-run convergence path
  - Calculate short-run effect on output with/without ZLB
- **(2C.) Larger primary deficit in the short run**, then bring debt back to steady state in long run by **exponentially declining adjustment of one fiscal instrument**
  - Fix long-run half-life of deviations from steady state
  - Calculate long-run convergence path
  - Calculate short-run effect on output with/without ZLB

# Comments on the scenarios compared

- To simplify the algebra, changes in interest payments are assumed financed by lump sum taxes
- Considering this simplification, is it really necessary to distinguish these two?

$$(2B): \quad \hat{b}_t - \hat{b}_{t-1} = \epsilon \quad (1)$$

$$(2C): \quad \hat{b}_t - \hat{b}_{t-1} - \frac{\bar{i}\bar{Y}}{\bar{b}}\hat{b}_{t-1} = \epsilon \quad (2)$$

- A more informative alternative might be:  
**(2D.) Lower lump-sum taxes in the short run**, then bring debt back to steady state in long run by **exponentially declining adjustment of one fiscal instrument**
  - Fix long-run half-life of deviations from steady state
  - Calculate long-run convergence path
  - Calculate short-run effect on output with/without ZLB

# Putting the pieces together

Now study a short-run change in government spending financed by long-run adjustments in spending or distorting taxes.

- **Short-run output effect of changing government spending**
  - ≈ Direct effect of spending now on output now
  - + Effect of spending now on deficit now
  - × Effect on output now of paying off later one unit of deficit now (conditional on instruments chosen to pay down the debt)
- That is:

$$\left. \frac{\Delta Y_t}{\Delta G_t} \right|_{TOTAL, \tau'} \approx \left. \frac{\Delta Y_t}{\Delta G_t} \right|_{(1)} + \left. \frac{\Delta D_t}{\Delta G_t} \right|_{(1)} \times \left. \frac{\Delta Y_t}{\Delta D_t} \right|_{(2C), \tau'}$$



# Calculations for Great Depression ( $i = 0$ )

- **Short-run output effect of raising government spending**  
(conditional on lowering government spending later)

$$\begin{aligned}\frac{\Delta Y_t}{\Delta G_t} \Big|_{TOTAL,G} &\approx \frac{\Delta Y_t}{\Delta G_t} \Big|_{(1)} + \frac{\Delta D_t}{\Delta G_t} \Big|_{(1)} \times \frac{\Delta Y_t}{\Delta D_t} \Big|_{(2C),G} \\ &\approx 2.2 - 0.3 \times 1.8 = 1.7\end{aligned}$$

- **Short-run output effect of raising government spending**  
(conditional on raising income taxes later)

$$\begin{aligned}\frac{\Delta Y_t}{\Delta G_t} \Big|_{TOTAL,\tau'} &\approx \frac{\Delta Y_t}{\Delta G_t} \Big|_{(1)} + \frac{\Delta D_t}{\Delta G_t} \Big|_{(1)} \times \frac{\Delta Y_t}{\Delta D_t} \Big|_{(2C),\tau'} \\ &\approx 2.2 - 0.3 \times (-1.9) = 2.8\end{aligned}$$

- **Short-run output effect of raising government spending**  
(conditional on raising income taxes later)

$$\approx 2.2 - 0.3 \times 2.2 = 1.5$$

# Is this an approximation?

- The formula might seem to have a chain rule in it, but it does not.
- Formula assumes the deficit that must be paid off is the one that would result **if the deficit were to be paid off using lump sum taxes.**
- Is there any reason to assume that the initial deficit occurring under lump-sum tax financing is approximately equal to the one occurring under distortionary financing?

# Alternative decompositions

Consider:

B. History with  $\Delta G_{SR} > 0$   
financed by lump sums

A. Baseline  
history

C. History with  $\Delta G_{SR} > 0$   
financed by  $\Delta G_{LR} < 0$

D. History with  $\text{lumps}_{SR} < 0$   
financed by  $\Delta G_{LR} < 0$

- Approximation says:

$$\Delta Y_{A \rightarrow C} \approx \Delta Y_{A \rightarrow B} + \Delta D_{A \rightarrow B} \times \frac{\Delta Y_{A \rightarrow D}}{\Delta D_{A \rightarrow D}}$$

- Why should that be a good approximation?

# Alternative decompositions

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- Exact depreciation is simply

$$\Delta Y_{A \rightarrow C} = \Delta Y_{A \rightarrow B} + \Delta Y_{B \rightarrow C}$$

- Can't  $\Delta Y_{B \rightarrow C}$  be calculated analytically in this model (working backwards from LR equilibrium)?

# The bigger picture

- Analytically tractable expressions for fiscal multipliers in standard textbook model are a valuable contribution
- Change at ZLB is strikingly large
- Important warning: in short run, **public spending reductions may cause higher deficits!**
- Nonetheless, let's remember that the effects of short-run adjustments are **not** the most important issue for Europeans to debate right now.
- For the Eurozone to function, member states must act to **ensure their long-run solvency**
  - What kinds of fiscal rules guarantee long-run solvency?
  - What structural reforms can get growth moving?
- “Austerity” is crucial, but the truly relevant constraint is the **intertemporal budget constraint**, not the short-run deficit *per se*.